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Impedance characteristics of deep brain stimulation electrodes *in vitro* and *in vivo*

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Abstract

The objective of this study was to quantify the electrode-tissue interface impedance of electrodes used for deep brain stimulation (DBS). We measured the impedance of DBS electrodes using electrochemical impedance spectroscopy in vitro in a carbonate- and phosphate-buffered saline solution and *in vivo* following acute implantation in the brain. The components of the impedance, including the series resistance (R_s) , the Faradaic resistance (R_f) and the double layer capacitance (C_{dl}) , were estimated using an equivalent electrical circuit. Both $R_{\rm f}$ and $C_{\rm dl}$ decreased as the sinusoidal frequency was increased, but the ratio of the capacitive charge transfer to the Faradaic charge transfer was relatively insensitive to the change of frequency. $R_{\rm f}$ decreased and $C_{\rm dl}$ increased as the current density was increased, and above a critical current density the interface impedance became nonlinear. Thus, the magnitude of the interface impedance was strongly dependent on the intensity (pulse amplitude and duration) of stimulation. The temporal dependence and spatial non-uniformity of $R_{\rm f}$ and $C_{\rm dl}$ suggested that a distributed network, with each element of the network having dynamics tailored to a specific stimulus waveform, is required to describe adequately the impedance of the DBS electrode-tissue interface. Voltage transients to biphasic square current pulses were measured and suggested that the electrode-tissue interface did not operate in a linear range at clinically relevant current amplitudes, and that the assumption of the DBS electrode being ideally polarizable was not valid under clinical stimulating conditions.

1. Introduction

Deep brain stimulation (DBS) for the treatment of neurological disorders is delivered from a four-contact electrode array implanted in the thalamus or basal ganglia. The efficacy of DBS is dependent on localizing charge delivery to specific populations of neurons, and charge delivery is influenced by the electrode-tissue interface, where a transduction of charge carriers occurs from electrons in the metal electrode to ions in the tissue. Characterizing the impedance of the DBS electrode-tissue interface is required to determine the charge delivery to the brain. For example, the interface capacitance modified the volume of neural activation by deep brain stimulation (Butson and McIntyre 2005). Further, the interface impedance contributes to the distribution of current density on the electrode, which may influence neural excitation, tissue damage and electrode corrosion during DBS. The purpose of this study was to quantify the impedance of the electrodeelectrolyte interface of deep brain stimulation electrodes both *in vitro* and *in vivo*.

The impedance of deep brain stimulation electrodes was characterized using electrochemical impedance spectroscopy (EIS) in vitro in a carbonate- and phosphate-buffered saline solution and in vivo following acute implantation in the brain. From the impedance spectrum, it is possible to deduce an equivalent electrical circuit model and match the circuit components to the physical characteristic of the interface. In a simple case, the interface can be modeled by a Randles circuit (Randles 1947), composed of a double-layer capacitor in parallel with the series combination of a charge-transfer resistance (Faradaic resistance) and a Warburg impedance (figure 1(a)). The Warburg impedance, which accounts for mass transfer limitations by diffusion, is negligible at high frequencies when the timescale is so short that diffusion does not influence reactions at the interface, or if the concentrations of reactants are high. It was determined experimentally that,



Figure 1. (a) The Randles equivalent circuit representation of the electrode–electrolyte interface. It is comprised of the double-layer capacitance $C_{\rm dl}$ in parallel with the series combination of a charge transfer Faradaic resistance $R_{\rm f}$ and the Warburg impedance W. (b) The simplified equivalent circuit model of the electrode–electrolyte interface, which is valid when the Warburg impedance is negligible.

under the frequencies and concentration used in this study, the Warburg impedance was negligible, and the equivalent model was reduced to the parallel combination of the double-layer capacitance C_{dl} and the Faradaic resistance R_f (figure 1(b)). Our results indicate that the double-layer capacitance and Faradaic resistance both decreased as the sinusoidal frequency was increased, and the double-layer capacitance increased and Faradaic resistance decreased as the current density was increased.

2. Methods

The impedance properties of clinical DBS electrodes (Model 3387, Medtronic Inc., MN, USA) were measured in vivo following acute implantation in the cat brain and in vitro in a near-physiological saline electrolyte buffered with carbonate and phosphate at concentrations found in interstitial fluid (137 mM NaCl, 29 mM NaHCO₃, 1.7 mM Na₂HPO₄ and 0.7 mM NaH₂PO₄) infused with a mixture of gas (5% CO₂, 6% O2 and 89% N2) to maintain a pH of 7.4 (Cogan et al 2004). The clinical DBS electrode (Model 3387) includes a linear array of four cylindrical electrode contacts (1.5 mm length, 1.27 mm diameter, 5.98 mm² surface area) separated by insulating rings (1.5 mm length). Impedance was measured with sinusoidal currents at 41 frequencies evenly distributed on a log scale between 1 Hz and 10 kHz, and at five rootmean-square amplitudes of 0.01 mA, 0.02 mA, 0.05 mA, 0.1 mA and 0.2 mA. The voltage transients generated by applying symmetrical biphasic square currents (200 μ s per phase and 1 ms per phase) were measured at 9 amplitudes from 0.01 mA to 5 mA. The measurements were replicated three times at each amplitude level for each of the four electrode contacts.

2.1. In vitro measurements

The three-electrode technique was used to measure impedance *in vitro* with an impedance analyzer (Model 1287 electrochemical interface (ECI) + Model 1252 frequency response analyzer (FRA), Solatron Analytical, Hampshire, UK) (figure 2). The electrode was placed vertically in the middle of a 200 ml beaker of a buffered saline solution at room



Figure 2. Experimental setup used to measure the impedance of DBS electrode and voltage transients generated by square currents. Abbreviations used in figure: CE—counter electrode, WE—working electrode, RE—reference electrode, ECI—electrochemical interface and FRA—frequency response analyzer.

temperature ($T \approx 20$ °C). Sinusoidal currents were applied between one contact of the DBS electrode (working electrode) and a counter electrode formed of a stainless steel wire spiraling around the wall of the beaker. The resulting potential between the working electrode and a silver/silver chloride reference electrode (Model RE-5B, BAS Inc., West Lafayette, IN, USA) was measured with the 1287 ECI (input impedance 10 G Ω in parallel with 50 pF). The impedance was calculated by dividing the measured potential by the applied current and included the electrode-electrolyte interface impedance in addition to the series resistance, $R_{\rm s}$. The series resistance included the solution (in vitro) or tissue (in vivo) resistance between the working electrode and the reference electrode, plus the electrical resistance of the lead wire, which was $40 \pm 1 \ \Omega$ (n = 4). This series resistance was minimized by positioning the reference electrode within 5 mm of the working electrode.

The same three-electrode cell was also used to measure voltage transients generated by symmetrical biphasic square currents delivered between the working electrode and the counter electrode. Voltage transients were measured between the DBS electrode and the reference electrode with an isolated differential amplifier (input impedance 100 M Ω in parallel with 25 pF, frequency response ±0.5 dB to 1 MHz, Model SR560, Stanford Research Systems, Sunnyvale, CA, USA), captured via a GPIB-equipped oscilloscope at a sampling rate of 1 MHz, and transferred to a computer for storage and analysis (figure 2, inside the dashed box).

2.2. In vivo measurements

Acute experiments were conducted in three adult male cats using the same instrumentation and methods used for the in vitro measurements. All animal care and experimental procedures were approved by the Institutional Animal Care and Use Committee of Duke University. Anesthesia was induced with ketamine HCl (Ketaset $35 \text{ mg kg}^{-1}\text{IM}$, supplemented as required during surgical preparation) and maintained with alpha-chloralose (65 mg kg^{-1} IV, supplemented at 15 mg kg⁻¹). The anesthesia level was determined by monitoring the blood pressure, heart rate, and withdrawal and blink reflexes. Body temperature was maintained between 37° and 39 °C with a water-circulating heating pad and warm 0.9% saline with 8.4 mg cc^{-1} sodium bicarbonate and 5% dextrose added was administered intravenously (~15 cc kg⁻¹ h⁻¹). The head was held in an upright position using a stereotaxic frame. A 1-2 cm diameter craniotomy was made on the top of the skull, and the dura was reflected to expose the underlying cortex. The DBS lead was inserted vertically into the neocortex, with the distal contact ~ 2 cm and the proximal contact \sim 1 cm beneath the brain surface. The stylet inside the lead, which ensured that the lead was stiff enough to penetrate the tissue, was then removed so that the lead could move with the brain tissue. The cortex was covered with surgical gauze soaked with physiological saline, and the reference electrode was positioned atop the gauze within 5 mm of the DBS lead. Thus, the distance from the active contact to the reference electrode varied from ~ 11 mm to ~ 21 mm. The large-area stainless steel surgical retractor was used as the counter electrode. Impedance spectrograms and voltage transients were measured in vivo using the three-electrode technique at the same amplitudes, frequencies and repetitions as the in vitro measurements, except biphasic current pulse amplitudes were limited to ≤ 2 mA, as larger currents evoked strong motor responses.

2.3. Impedance characterization

2.3.1. Impedance characterization with sinusoidal currents. The measured impedance data were used to estimate the element values of a three-element equivalent circuit model including the parallel combination of $R_{\rm f}$ and $C_{\rm dl}$ in series with $R_{\rm s}$:

$$Z(\omega) = R_{\rm s} + \frac{R_{\rm f}}{1 + j\omega R_{\rm f} C_{\rm dl}}$$

= $R_{\rm s} + \frac{R_{\rm f}}{1 + (\omega R_{\rm f} C_{\rm dl})^2} - j \frac{\omega R_{\rm f}^2 C_{\rm dl}}{1 + (\omega R_{\rm f} C_{\rm dl})^2}$
= $Z'(\omega) + j Z''(\omega)$,

where ω is the angular frequency, Z' is the real part of impedance and Z'' is the imaginary part of impedance. Since charge transfer through the electrode–electrolyte interface was shunted by the double-layer capacitance at very high frequency, series resistance R_s was determined as the asymptotic high frequency impedance

$$R_{\rm s} = Z(f \to \infty).$$

The series resistance R_s was subtracted from the real part of impedance, and R_f and C_{dl} at each frequency were determined as

$$R_{\rm f}(\omega) = \frac{Z''^2 + (Z' - R_{\rm s})^2}{Z' - R_{\rm s}},$$
$$C_{\rm dl}(\omega) = -\frac{Z''}{\omega[(Z' - R_{\rm s})^2 + Z''^2]}.$$

2.3.2. Impedance characterization with biphasic pulsed currents. In the voltage transient study, the element values of the three-element equivalent circuit model were determined by minimizing the sum of the squares of the residuals of the measured points minus the theoretical values. The theoretical voltage response to the biphasic square current pulses was described with the equations

$$V(t) = \begin{cases} \left(1 - \exp\left(-\frac{t}{R_{\rm f}C_{\rm dl}}\right)\right)I R_{\rm f} + I R_{\rm s} & 0 \leqslant t \leqslant {\rm PW} \\ \left(-1 + \exp\left(-\frac{t}{R_{\rm f}C_{\rm dl}}\right)\right)\left(-1 + 2\exp\left(\frac{{\rm PW}}{R_{\rm f}C_{\rm dl}}\right)\right)I R_{\rm f} \\ -I R_{\rm s} & {\rm PW} < t \leqslant 2\,{\rm PW} \\ -\exp\left(-\frac{t}{R_{\rm f}C_{\rm dl}}\right)\left(-1 + \exp\left(\frac{{\rm PW}}{R_{\rm f}C_{\rm dl}}\right)\right)^2 I R_{\rm f} & t > 2\,{\rm PW} \end{cases}$$

where *I* is the amplitude of the applied current and PW is the pulse width of the current pulse. The voltage transient at t > 2 PW represents the discharge of the double layer after the applied current returned to zero.

3. Results

We measured the impedance of deep brain stimulation electrodes with both sinusoidal and square currents *in vitro* in the buffered saline solution and *in vivo* following acute implantation in the brain. $R_{\rm f}$ and $C_{\rm dl}$ were quantified as functions of current density and frequency from the impedance spectra, and as a function of current density from the voltage transients.

3.1. Impedance characteristics

3.1.1. Impedance spectra. Impedance (amplitude and phase) spectra and impedance Nyquist plots measured in vitro and in vivo for a single DBS electrode contact at three current amplitudes are shown in figure 3. The measured impedance is composed of the electrode-electrolyte interface impedance, which dominates at low frequencies, and the series resistance, which dominates at high frequencies (Ragheb et al 1992). The asymptotic, high-frequency impedance resulting from the series resistance R_s was $119 \pm 7 \Omega$ (mean \pm SD, range = 107– 141 Ω , n = 60 (4 contacts \times 5 amplitudes \times 3 repetitions)) *in vitro* and 473 \pm 159 Ω (mean \pm SD, range = 260–928 Ω , n = 180 (4 contacts \times 5 amplitudes \times 3 repetitions \times 3 cats)) in vivo (figures 3(a), (d)). The phase of the impedance approached zero at high frequencies indicating that the high-frequency impedance was mainly resistive (figures 3(b), (e)). The value of R_s can also be read from the Nyquist plots where the impedance loci intersect the abscissa



Figure 3. Impedance magnitude spectra of the DBS electrode *in vitro* (a) and *in vivo* (d) measured at 41 frequencies evenly distributed on a log scale from 1 Hz to 10 kHz with sinusoidal currents at root-mean-square amplitudes of 0.01 mA, 0.05 mA and 0.2 mA. Impedance phase spectra of the DBS electrode *in vitro* (b) and *in vivo* (e) at amplitudes of 0.01 mA, 0.05 mA and 0.2 mA. Nyquist plots of the real and imaginary parts of the DBS electrode impedance *in vitro* (c) and *in vivo* (f) at amplitudes of 0.01 mA, 0.05 mA, 0.05 mA and 0.2 mA.

(figures 3(c), (f)). The difference between R_s in vitro and R_s in vivo resulted from both the difference in the conductivities of the surrounding medium and the difference in the proximity of the reference electrode to the DBS contacts. The electrode–electrolyte interface impedance varied inversely with frequency—in the k Ω range at 1 Hz decreasing to almost zero at 10 kHz. At low frequencies (<100 Hz), the interface impedance also varied inversely with the current amplitude, both *in vitro* (figure 3(a)) and *in vivo* (figure 3(d)).

3.1.2. Changes of R_f and C_{dl} with frequency. The Faradaic resistance R_f and double-layer capacitance C_{dl} calculated from the impedance spectra *in vitro* and *in vivo* are shown in figure 4. Both R_f and C_{dl} decreased monotonically with increasing frequency from 1 to 10 kHz both *in vitro* and *in vivo*. R_f and C_{dl} were strongly dependent on the current amplitude at low frequencies (<100 Hz), but not at high frequencies (>100 Hz).

3.1.3. Changes of $R_{\rm f}$ and $C_{\rm dl}$ with current density. $R_{\rm f}$ and $C_{\rm dl}$ were dependent on the current density, as well as the frequency (Dymond 1976, Geddes 1997, Onaral and



Figure 4. Faradaic resistance (R_f) as a function of frequency *in vitro* (a) and *in vivo* (c). Double layer capacitance (C_{dl}) as a function of frequency *in vitro* (b) and *in vivo* (d). Note that only the upper error bars were plotted at 0.2 mA in (c) because the lower error bar at some frequencies extended beyond the lower range of the log scale.



Figure 5. Faradaic resistance, R_f , as a function of current density at different frequencies *in vitro* (a) and *in vivo* (c). Double layer capacitance, C_{dl} , as a function of current density at different frequencies *in vitro* (b) and *in vivo* (d). Values are means across 12 trials (4 contacts × 3 repetitions) *in vitro* and 36 trials (4 contacts × 3 repetitions) *in vivo*.

Schwan 1982, Ragheb and Geddes 1990). To illustrate this dependency, R_f and C_{dl} were plotted versus average current density (rms current divided by the electrode surface area) at different frequencies (figure 5). In the low frequency range, R_f decreased and C_{dl} increased when the current density increased above a certain value. Previous studies identified the 'current density linearity limit' as the current density at which the values of *R* or *C* deviated by 10% from those observed at low current densities (Geddes 1997, Onaral and Schwan 1982, Ragheb and Geddes 1990). At low frequencies (<100 Hz)



Figure 6. *In vivo* voltage responses (gray) to symmetrical biphasic square currents (1 ms per phase) at different amplitudes between 0.01 mA and 2 mA, and the least-square curve fits (black) to the voltage responses. The correlation coefficients (r^2) are 0.990, 0.994, 0.996, 0.996, 0.996, 0.996, 0.996, 0.996, 0.996, 0.996, 0.994 and 0.994, respectively, from 0.01 mA to 2 mA. Open circuit potential was 0.34 ± 0.14 V (n = 36, 4 contacts × 9 amplitudes) *in vitro* and 0.38 ± 0.23 V (n = 96, 4 contacts × 8 amplitudes × 3 cats) *in vivo*.



Figure 7. Values of the three elements of the equivalent electrical circuit estimated from the voltage responses to biphasic current pulses *in vitro* and *in vivo*. (a) Series resistance, R_s , as a function of current amplitude of the square pulses. (b) Faradaic resistance, R_f , as a function of current amplitude of the square pulses. (c) Double-layer capacitance, C_{dl} , as a function of current amplitude of the square pulses.

 $R_{\rm f}$ and $C_{\rm dl}$ also exhibited a current density linearity limit, which was approximately 0.334 mA cm⁻², corresponding to a stimulus current of 0.02 mA, but this linearity limit was not evident at frequencies >100 Hz.

3.2. Voltage transients in response to biphasic current pulses

Examples of the voltage responses to symmetrical biphasic square current pulses with different amplitudes and the corresponding least-square regression fits to the data are shown in figure 6. The fits matched the measured data well at low current amplitudes, while stronger deviations between the fits and measurements appeared at higher current amplitudes. Increasing deviation at higher currents indicated that the electrode–electrolyte interface no longer operated in a linear range at high currents, and therefore could not be fit as well with a linear circuit. Gas bubbles formed on the surface of the DBS electrode during the *in vitro* measurements at current amplitudes above 1 mA, indicating the occurrence of water hydrolysis.

The average values of R_s , R_f and C_{dl} estimated from the voltage transient data are shown in figure 7 as a function of current amplitude. The values of R_s were consistent across

current amplitudes both *in vitro* (mean \pm SD = 133 \pm 7 Ω , range = 123–150 Ω , *n* = 36) and *in vivo* (mean \pm SD = 533 \pm 152 Ω , range = 335–920 Ω , *n* = 96) and were comparable to the R_s values calculated from the impedance spectra. The values of R_f and C_{dl} were constant at low currents but deviated from these values when the current amplitude increased. These changes, however, cannot be readily compared with the changes of R_f and C_{dl} with current calculated from impedance spectra (figure 5) because fitting the voltage transients with a linear model assumed that R_f and C_{dl} did not change during the time course of the current pulse. This is not a valid assumption because the data from the impedance spectra demonstrated that R_f and C_{dl} changed with frequency (figure 4).

4. Discussion

The goal of this study was to quantify the impedance of deep brain stimulation electrodes *in vitro* and *in vivo*. Characterizing the electrode impedance enables the differentiation of the charge injection pathways through the electrode–electrolyte interface. Charge transfer at the electrode–electrolyte interface can be in the form of the



Figure 8. The ratio of capacitive charge transfer to Faradaic charge transfer as a function of frequency *in vitro* (a) and *in vivo* (b).

capacitive (non-Faradaic) charge transfer, Q_c , or the resistive (Faradaic) charge transfer, Q_f . The ratio of the two forms of the charge transfer Q_c/Q_f is an index for evaluating the propensity for stimulation to cause electrode or tissue damage. The charge transfer ratio Q_c/Q_f (figure 8) was calculated from the data in figure 4 as

$$\frac{Q_{\rm c}}{Q_{\rm f}} = \frac{i_{\rm c}}{i_{\rm f}} = j\omega R_{\rm f} C_{\rm dl} = j \cdot 2\pi f \cdot R_{\rm f} C_{\rm dl}.$$

If $R_{\rm f}$ and $C_{\rm dl}$ were independent of frequency, then $Q_{\rm c}/Q_{\rm f}$ would increase in proportion to the frequency, and stimulation waveforms with strong high-frequency components (such as short pulse widths) could make the electrode highly polarizable by transferring charge mainly in the capacitive form. Our results indicate that $R_{\rm f}$ and $C_{\rm dl}$ both decreased monotonically with increasing frequency (figure 4), and, as a result, the ratio of the capacitive charge transfer to the Faradaic charge transfer was relatively insensitive to the frequency (figure 8). Q_c/Q_f was $\sim 2-3$ times larger *in vitro* than *in vivo*, suggesting that the non-Faradaic (capacitive) charge capacity of DBS electrodes was overestimated by the in vitro measurements, presumably due to differences in chemical composition between the in vitro and in vivo environments (Onaral and Schwan 1982). Further, the quantification of $R_{\rm f}$ and $C_{\rm dl}$ in vivo may have been influenced by the larger and more variable series resistance.

The interface impedance influences the distribution of current density on the electrode surface. The edge effect describes that the current density increases toward the perimeter of the electrode (Newman 1966) and is an important factor that affects the patterns of neural excitation (McIntyre and Grill 2001, Wei and Grill 2005) and tissue damage (McCreery et al 1990). Our results demonstrate that $R_{\rm f}$ decreased and $C_{\rm dl}$ increased with increasing current density (figure 5), and this resulted in a decrease of the magnitude of the interface impedance with increasing current density (figures 3(a), (d)). This suggests that the nonuniform distribution of current density will result in a nonuniform interface impedance with the interface impedance decreasing toward the perimeter of the electrode. Further, the decrease of $R_{\rm f}$ and the increase of $C_{\rm dl}$ with increasing current density occurred when the rms current was above 0.02 mA (section 3.1.2). Typical DBS parameters of 2 V, 90 μ s pulse width, and 165 Hz (Kuncel and Grill 2004) yielded the peak current of 1.76 mA and the rms current of 0.23 mA measured with the three-electrode technique in the brain, much higher than the identified current linearity limit of 0.02 mA, and indicating that the DBS electrode–tissue interface may operate in a nonlinear fashion during effective DBS therapy.

A number of mechanisms may underlie the dependence of interface resistance and capacitance on frequency and current density. The monotonic decrease of Faradaic resistance with increasing frequency may reflect that at high frequencies the voltage polarity across the electrode changes so rapidly that the electrochemical reactants for the reactions to be reversed are more readily available adjacent to the electrode surface (i.e. there is insufficient time for diffusion). The decrease of Faradiac resistance with increasing current density, seen when electrode entered the nonlinear region, is due to the initiation of new reaction mechanisms at the electrode surface, capable of accommodating the increased current beyond the limits of the available reacting species. The frequency dependence of double-layer capacitance was suggested to be a result of the relaxation of absorbed water dipoles, which act as a dielectric in the double-layer capacitance (Bockris and Conway 1958). The increase of double-layer capacitance with increasing current density, seen when electrode entered the nonlinear region, is possibly due to the increased fraction of the electrode surface covered by adsorbed chemical species such as halide anions and polar molecules such as water, with a preferential orientation at the interface acting to separate charge (Conway 1965, Dymond 1976).

4.1. Equivalent electrical circuit models of the interface impedance

We modeled the interface impedance with the parallel combination of a resistor and a capacitor; this representation has also been used by other investigators (Gileadi et al 1975, Robinson 1968, Yoo and Park 2000). However, the interface impedance may also be modeled by the series combination of a resistor and a capacitor (Onaral and Schwan 1982, Ragheb and Geddes 1990, Ragheb et al 1992 and Schwan 1968), and the dependence of interface resistance and capacitance on frequency and current density are well documented using this series representation. Both the series resistance and capacitance decreased with increasing frequency for a platinum electrode in 0.9% saline over the frequency range of 0.001-1000 Hz (Onaral and Schwan 1982), and at 100 Hz the series resistance decreased and the series capacitance increased with increasing current density (Schwan 1968). Similarly, for a large number of metals, the series resistance decreased and the series capacitance increased with increasing current density, but these changes were not pronounced at low current densities (Ragheb and Geddes 1990). Schwan first defined a 'limit current of linearity' as the current at which the values of series resistance and capacitance deviated by 10% from the values observed at low current density (Schwan 1968).

Our results, modeling the interface with the parallel combination of a resistor and a capacitor, revealed changes in the parallel resistance and capacitance with frequency and current density similar to those of the series resistance and capacitance. The changes of parallel components $R_{\rm f}$ and $C_{\rm dl}$ with frequency and current density have not been previously

reported. Under Warburg's assumption of a constant phase angle, the parallel and series circuits are equivalent, and the conversion from one circuit to the other is a simple scale factor (see the appendix). Hence, the parallel components $R_{\rm f}$ and $C_{\rm dl}$ follow the same trends with the change of frequency and current density as the series components, with exceptions at very low frequencies where Warburg's assumption breaks down (see the appendix).

4.2. Limitations of experiments

We measured the impedance of deep brain stimulation electrodes by applying sinusoidal currents in vitro in a buffered saline solution and in vivo following acute implantation in the brain. $R_{\rm f}$ and $C_{\rm dl}$ were determined as the functions of both current density and frequency by fitting an electrical circuit equivalent model to the impedance spectrograms. One limitation of this approach is that the current density was spatially averaged over the geometric area of the electrode when quantifying the changes of $R_{\rm f}$ and $C_{\rm dl}$ with the current density. However, the current density varies over the surface of an electrode, and to obtain a relationship between $R_{\rm f}$ and $C_{\rm dl}$ and the absolute current density requires an electrode with uniform current density on the electrode surface (Ksienski 1992, Rubinstein et al 1987, Wiley and Webster 1982). Second, spatially lumped circuit elements were used to describe spatially distributed interface parameters. However, the lumped circuit model allowed the parameterization of the interface impedance using a limited number of circuit elements that have clear physical representations. Third, this study quantified the electrode-tissue interface impedance of clinical DBS electrodes in vivo in the cat brain, while the DBS electrodes were designed for human brains. The smaller size of the cat brain did not permit precise positioning of the electrode in a specific region of the brain. Further, the acute nature of the *in vivo* experiment did not allow the investigation of the post-operative changes in impedance that may accompany the chronic foreign body reaction to the electrode (Grill and Mortimer 1994, Williams et al 2007).

4.3. Implications for modeling of deep brain stimulation electrodes

The quantitative description of DBS electrode-electrolyte interface impedance from experimental measurement has not been previously documented. Holsheimer et al measured the impedance of the DBS electrode in vitro in a physiological saline with monophasic rectangular voltage pulses (Holsheimer et al 2000). The 'impedance' they measured was the instantaneous impedance calculated by dividing the amplitude of the rectangular voltage by the instantaneous current. This does not allow the characterization of the charge-transfer processes at the interface through the Faradaic resistance or the double-layer capacitance. Using the data from Holsheimer et al, Butson and McIntyre assumed that the DBS electrode was ideally polarizable and included only a capacitance to represent the interface impedance (Butson and McIntyre 2005). A highly polarizable (real) electrode can accommodate a large amount of charge on the double layer prior to initiating Faradaic reactions, and thus is highly desirable for stimulation. However, it is necessary to determine whether such a model is representative of the DBS electrode under clinical stimulating conditions.

Considering the series resistance present in the threeelectrode measurement scheme, the equivalent circuit of an ideally polarizable electrode is a capacitor in series with the series resistance. At constant current, the potential across the ideally polarizable electrode changes linearly with time according to

$$V(t) = \frac{1}{C} \int_0^t I \cdot \mathrm{d}T = \frac{I \cdot t}{C},$$

if C does not change over time. The voltage responses to 0.02 mA, 0.2 mA and 2 mA biphasic current pulses were scaled and plotted in figure 9, along with the voltage waveform for an ideally polarizable electrode in series with R_s . The capacitance of the ideally polarizable electrode was chosen to match the initial slope (at t = 0+) of the voltage waveforms of the DBS electrode because current was purely capacitive upon pulsing and the instantaneous capacitance at t = 0+ is proportional to the inverse of the initial slope. These values, 0.8 μ F in vivo and 1.6 μ F in vitro, are also similar to the values obtained by fitting the in vivo and in vitro measurements at low currents (figure 7(c)). The voltage response of the real electrode deviated from that of the ideally polarizable electrode and the deviation increased as the amplitude and duration of the current increased (figure 9), indicating that a larger fraction of charge was transferred through Faradaic reactions. Further, for the ideally polarizable electrode, the electrode potential returned to the open circuit potential after the charge-balanced biphasic pulse because the charge in the first phase was fully recovered during the second phase. For the real electrode, not all of the charge injected during the first (anodic) phase went into charging of the double layer, and only some fraction of the charge in the second (cathodic) phase was required to discharge the double layer. The 'extra' cathodic charge resulted in a post-pulse electrode potential negative of the pre-pulse value (figure 9), and the opposite was observed for cathodic-first biphasic pulses. Thus, the DBS electrode is not ideally polarizable under clinical stimulating conditions.

Charge per phase and charge density per phase are cofactors in determining stimulation-induced tissue damage (McCreery et al 1990, 1988). The charge per phase limit 1.8 μ C and geometrical charge density limit 30 μ C cm⁻² for DBS electrode (Kuncel and Grill 2004) were extracted from previous studies on charge, charge density and tissue damage (Agnew et al 1983, Brown et al 1977, McCreery et al 1990, 1988, Pudenz et al 1975, Yuen et al 1981). In our transient pulse study, the charge per phase ranged from 0.002 μ C (for the 0.01 mA, 0.2 ms pulse) to 2 μ C (for the 2 mA, 1 ms pulse), which covered the identified charge limit of 1.8 μ C. The voltage transients suggest a pronounced deviation from a linear model at charge per phase over 1 μ C and gas bubble formation was observed above 1 μ C. This indicates that the charge per phase limit of 1.8 μ C extracted from previous studies may not be conservative enough and irreversible Faradic reactions



Figure 9. Voltage responses to biphasic current pulses at various amplitudes. (a) *In vivo* voltage responses to symmetrical biphasic square current with 1 ms pulse width at amplitudes of 0.02 mA, 0.2 mA and 2 mA (from figure 6) and the voltage response of an ideally polarizable electrode (0.8 μ F) in series with tissue resistance (520 Ω) to square current at 2 mA. (b) *In vitro* voltage responses to symmetrical biphasic square current with 200 μ s pulse width at amplitudes of 0.02 mA, 0.2 mA and 2 mA and 2 mA and the voltage response to an ideally polarizable electrode (1.6 μ F) in series with tissue resistance (120 Ω) to square current at 2 mA. The waveform in response to 0.02 mA current was scaled by a factor of 100 and the waveform in response to 0.2 mA current waveform in response to 2 mA current.

may be initiated below this limit. The appearance of the voltage transients suggests that the gas bubbling was a result of hydrogen evolution in the cathodic phase of the pulse, because the voltage deviated more prominently at high current amplitudes in the cathodic phase than in the anodic phase and the potential excursion exceeded the potential (-0.22 V versus Ag-AgCl (Robblee and Rose 1990)) that initiates the reduction of water (figure 6).

The results of this study provide parameters required to include accurate representations of the electrode–tissue interface in computational models of DBS. However, the nonlinear dependence of both R_f and C_{dl} on frequency and current density poses a challenge to incorporate readily the interface impedance into models. Because the current density distribution on the electrode is spatially non-uniform, with higher current density at the edges than in the center of the electrode (Newman 1966), R_f and C_{dl} will vary spatially along the electrode–tissue interface. Further, because the frequency content of the stimulation pulse changes over the time course of the pulse, R_f and C_{dl} also vary temporally during the stimulation. Therefore, the interface impedance is best described by a distributed rather than a lumped parameter network, with each parameter of the network having dynamics tailored to the stimulus waveform.

In summary, this study utilized electrochemical impedance spectroscopy and transient pulse responses to characterize deep brain stimulation electrodes *in vitro* in the carbonate- and phosphate-buffered saline and *in vivo* following acute implantation in the brain. The electrode–tissue interface impedance operated in a nonlinear regime with clinically relevant current amplitudes, and the nonlinearity complicates incorporation of the interface impedance into models of DBS. The assumption of the DBS electrode being ideally polarizable is not valid under clinical stimulating conditions, indicating the occurrence of the Faradaic charge transfer through the electrode–tissue interface. It awaits further investigation to identify the electrochemical reactions contributing to the Faradaic charge transfer.

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Appendix

The impedance of the parallel combination of $R_{\rm f}$ and $C_{\rm dl}$ is

$$Z_p(\omega) = \frac{R_{\rm f}}{1 + (\omega R_{\rm f} C_{\rm dl})^2} - \frac{j \omega R_{\rm f}^2 C_{\rm dl}}{1 + (\omega R_{\rm f} C_{\rm dl})^2}.$$

For the series combination of a resistor R_w and capacitor C_w , the impedance is

$$Z_{\rm s}(\omega) = R_{\rm w} - \frac{\rm j}{\omega C_{\rm w}}$$

Both models are intended to represent the same physical system and thus $Z_p(\omega) = Z_s(\omega)$. This equality yields

$$R_{\rm f} = R_{\rm w} \left(1 + \frac{1}{(\omega R_{\rm w} C_{\rm w})^2} \right)$$
$$C_{\rm dl} = \frac{C_{\rm w}}{1 + (\omega R_{\rm w} C_{\rm w})^2}.$$

Warburg stated that at low current densities both R_w and C_w vary as the square root of frequency, $1/\sqrt{\omega}$ (Onaral and Schwan 1982, Ragheb and Geddes 1990). The consequence of this relationship is that the phase angle, which equals to $\tan^{-1}(\omega R_w C_w)$ is constant at 45° at all frequencies. For the special case $\omega R_w C_w = 1$, the above relations become

$$R_{\rm f} = 2R_{\rm w},$$
$$C_{\rm dl} = \frac{C_{\rm w}}{2}.$$

This indicates that parallel and series circuits become equivalent under Warburg's assumption, and the conversion from one circuit to the other is a simple factor of 2. However, the series representation of interface does not allow the passage of the direct current, and as ω approaches zero, the condition $\omega R_w C_w = 1$ breaks down. Thus, the parallel model is more appropriate at low frequencies than the series model.

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